PSYC402-week-18-LME-2

Rob Davies (Lancaster University)

Targets for Week 18 – Ideas and skills

- Practice how to tidy experimental data for mixed-effects analysis
- Begin to develop understanding of crossed random effects of subjects and stimuli
- Practice fitting linear mixed-effects models incorporating random effects of subjects and stimuli

To be modern psychological data analysts you will need to know the *what*, *why*, *when and how* of multilevel or mixed-effects models

This week, we make a *subtle* change and start talking more about Linear Mixed-effects models

Repeated measures data: we begin by *revising* our list of when we need mixed-effects models

- When we test the same people multiple times
 - Pre- and post-treatment
 - Multiple stimuli everyone sees the same stimuli
 - Repeated testing follow learning, development within individuals in longitudinal designs
- When we do multi-stage sampling
 - Find (sample) classes or schools test (sample) children within classes or schools
 - Find (sample) clinics test (sample) patients within clinics

Where we are going: linear mixed-effects models

- We need to learn how to estimate the effects of experimental variables
- while also taking into account sources of error variance like
 - the random differences between people we test
 - and the random differences between stimuli we present

The wider scientific impact – accepting diversity

- How do psychological effects vary?
- Uniformity is a common because convenient assumption
- We ask: How do people vary in their response?



The data we will work with: the CP study data

- As part of our lab work, we will practice steps often required to get data ready for mixed-effects model
- CP studied how 62 children read 160 words
- The data are in separate files and the files are untidy
 - CP study word naming rt 180211.dat reaction time for correct responses to word stimuli in reading
 - CP study word naming acc 180211.dat accuracy for all responses to word stimuli in reading
 - words.items.5 120714 150916.csv information about the 160 stimulus words presented in reading task
 - all.subjects 110614-050316-290518.csv information about the 62 participants

We will make data tidy

• What a horrible mess:

A tibble: 6 x 62

- Psychological data collection often delivers untidy data
- Here, we have data for different participants in separate columns
- Each row holds the reaction times for the responses made by all participants to each stimulus word
- Each cell holds the reaction time for the response made by a child to a word
- We have missing values NA and reaction times

```
##
     item_name AislingoC AlexB AllanaD AmyR AndyD AnnaF Aoife
##
     <chr>
                     <dbl> <dbl>
                                     <dbl> <dbl> <dbl> <dbl> <dbl>
                                                                 <db.
## 1 act
                      595.
                             586
                                       NA
                                            693
                                                   597
                                                          627
                                                                  649
## 2 ask
                      482.
                             864
                                     1163
                                            694.
                                                   616
                                                          631
                                                                  538
                      458.
                             670
                                     1114.
                                                  1019
                                                          796.
                                                                  54
## 3 both
                                            980
                                            678
                                                   589
                                                          604
## 4 box
                      546
                             749.
                                      975
                                                                  574
                      580
                                       NA
                                             789
                                                   684
                                                           NΑ
## 5 broad
                            1474.
                                                                  816
```

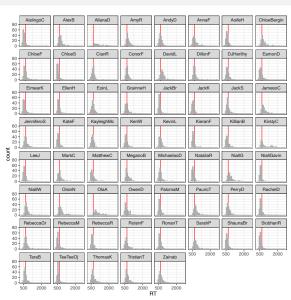
Next: When we do we need mixed-effects models?

When we do we need mixed-effects models? When we have repeated measures data

- In a reading study, we ask all individuals in a participant sample to read all words in a stimulus sample
- For each individual, we will have multiple observations and these observations will not be independent
 - One participant will tend to be slower or less accurate compared to another
 - Her responses may be more or less susceptible to the effects of the experimental variables
- The observed responses in different trials can be grouped by participants

Participants will vary for reasons we cannot explain

- Here you see a separate histogram plot for each participant
- Bars show the distribution of reaction time (RT)
- The red line shows the overall mean RT

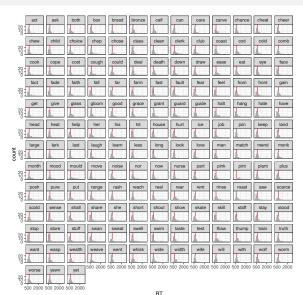


When we do we need mixed-effects models? When we have repeated measures data

- In a reading study, we ask all individuals in a participant sample to read all words in a stimulus sample
- For each stimulus, there are multiple observations and these observations will not be independent
 - One stimulus may prove to be more challenging to all participants compared to another, eliciting slower or less accurate responses
 - The effects of *within-items* experimental variables may be more or less prominent for responses to some stimuli than to others
- So the data can also be grouped by stimuli

Stimuli will vary for reasons we cannot explain

- Here you see a separate histogram plot for the responses to each word
- Bars show the distribution of reaction time (RT)
- The red line shows the overall mean RT



The language-as-fixed-effect fallacy

- If you are doing a repeated measures design study in which there are different participants
- And different tests or test items or stimuli
- And all participants respond to all stimuli
- Then you need to use mixed-effects models
- Because you need to deal with the random differences between people and the random differences between stimuli

The language as fixed effect fallacy

A very famous paper by Clark (1973)

- Historically, psychologists tested effects against error variance due to differences between people
- They ignored differences due to stimuli
- This meant they were likely to find significant effects not because there were true differences between conditions
- But because there were random differences between stimuli presented in different conditions

Taking into account error variance due to subjects and items – Clark's (1973) minF' solution

$$minF' = \frac{MS_{effect}}{MS_{random-subject-effects} + MS_{random-word-differences}} = \frac{F_1F_2}{F_1 + F_2}$$
(1)

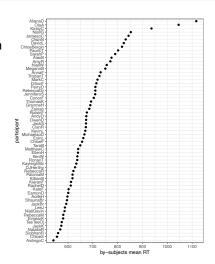
- You start by aggregating your data
 - By-subjects data for each subject, take the average of their responses to all the items
 - By-items data for each item, take the average of all subjects' responses to that item
- You do separate ANOVAs, one for by-subjects (F1) data and one for by-items (F2) data
- You put F1 and F2 together, calculating minF'

Using tidyverse functions, it is easy to calculate by-subjects and by-items RT averages

- We can then join the by-items data with stimulus properties and analyze the
 effects of those properties (e.g. word frequency)
- or we can join the by-subjects data with participant attributes and analyze the
 effects of those attributes (e.g. participant group)
- We cannot look at both item and participant effects at the same

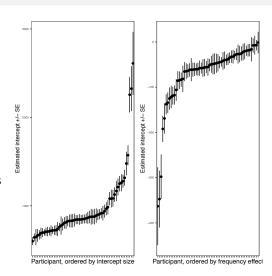
But analysing data only by-items means we lose track of participant differences

- Lorch & Myers (1990) warn: analyzing just by-items mean RTs assumes wrongly that subjects are a fixed effect
- We can see this is wrong because, for example, with the CP data, we can see that participant RT varies substantially



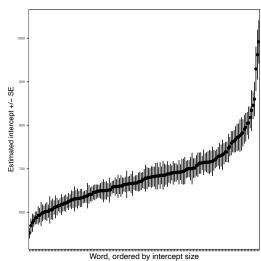
Participant differences in *both* average RT (or accuracy) and the impacts of effects

- These error bar plots show:
 - As points: the estimated intercept or the estimated effect of frequency on RT
 - Together with the standard errors of the estimates
 - For each participant analyzed separately
- We can see that participants vary greatly in both estimated intercept or slope and in uncertainty about estimates



Equally, analysing by-subjects data alone means we would lose track of random differences between stimuli

- These error bar plots show:
 - As points: the estimated intercept
 - Together with the standard errors of the estimate
 - For responses to each word analyzed separately
- We can see that responses to different words vary greatly in average speed - here, we ignore other effects



Next: So what do we do? We use mixed-effects models and we include random effects for both participants and stimuli

We account for differences between participants in intercept by modelling the intercept as two terms

$$\beta_{0i} = \gamma_0 + U_{0i} \tag{2}$$

- Where γ_0 is the average intercept
- And U_{0i} is the difference for each i child between their intercept and the average intercept

We account for differences between participants in slope by modelling the slope of effects as two terms

$$\beta_{1i} = \gamma_1 + U_{1i} \tag{3}$$

- Where γ_1 is the average slope
- And U_{1i} represents the difference for each i child between the slope of their frequency effect and the average slope

We account differences between items in intercepts by modelling the intercept as two terms

$$\beta_{0j} = \gamma_0 + W_{0j} \tag{4}$$

- Where γ_0 is the average intercept
- And W_{0j} represents the deviation, for each word, between the word intercept and the average intercept

Our model can now incorporate the random effects of *both* participants and words

$$Y_{ij} = \gamma_0 + \gamma_1 X_j + U_{0i} + U_{1i} X_j + W_{0j} + e_{ij}$$
 (5)

- Where the outcome Y_{ij} is related to ...
- The average intercept γ_0 and differences between i children in the intercept U_{0i} ;
- The average effect of the explanatory variable frequency $\gamma_1 X_j$ and differences between i participants in the slope $U_{1i}X_i$;
- Plus the random differences between items in intercepts W_{0i}
- And the residual error variance e_{ii} .

- Imer.all <- Imer(...) create a linear mixed-effects model object using the Imer() function
- RT ~ Lg.UK.CDcount the fixed effect in the model is expressed as a formula in which the outcome RT is predicted ~ by word frequency, given by Lg.UK.CDcount in the dataset
- We use data = long.all.noNAs to specify the data we are analyzing

- We add (...|subjectID) to specify random differences between sample groups (here, participants), specified using the dataset subjectID coding variable name
- We add (...1 |subjectID) to account for random differences between participants in intercepts, coded 1
- and (Lg.UK.CDcount ... |subjectID) to account for random differences between participants in the slope of the frequency effect, specified using the dataset Lg.UK.CDcount variable name

- We add the term (...|itemname) to specify random effects corresponding to random differences between sample groups (here, items) coded using the itemname variable name
- We add (1 | itemname) to account for random differences between sample groups (words) in intercepts, coded 1

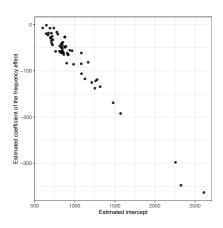
We usually do not aim to examine the specific deviations

We estimate just the *spread of deviations* by-participants or by-words: the **variance**

- $var(U_{0i})$ variance of deviations by-participants from the average intercept;
- $var(U_{1i}X_j)$ variance of deviations by-participants from the average slope of the frequency effect;
- $var(W_{0j})$ variance of deviations by-items from the average intercept;
- $var(e_{ij})$ residuals, at the response level, after taking into account all other terms.

Expect random effects will covary

- Participants who are slower to respond also show the frequency effect more strongly
- The scatterplot shows the relationship between per-participant estimates of
- The intercept and the slope
- The strong relationship is clear



How do you report a mixed-effects model?

```
## Linear mixed model fit by REML. t-tests use Satterthwaite's method [
## lmerModLmerTest]
## Formula: RT ~ Lg.UK.CDcount + (Lg.UK.CDcount + 1 | | subjectID) + (1 |
      item_name)
     Data: long.all.noNAs
## REML criterion at convergence: 116976.7
##
## Scaled residuals:
      Min
             1Q Median 3Q
                                    Max
## -4.1794 -0.5474 -0.1646 0.3058 12.9485
##
## Random effects:
                          Variance Std.Dev.
## Groups Name
## item name (Intercept)
                            3397 58.29
## subjectID Lg.UK.CDcount 3623 60.20
## subjectID.1 (Intercept) 112307 335.12
## Residual
                             20704 143.89
## Number of obs: 9085, groups: item name, 159; subjectID, 61
##
## Fixed effects:
##
               Estimate Std. Error df t value Pr(>|t|)
## (Intercept) 971.07 51.86 94.62 18.723 < 2e-16 ***
## Lg.UK.CDcount -72.33 10.79 125.27 -6.703 6.23e-10 ***
## ---
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' ' 1
##
## Correlation of Fixed Effects:
##
              (Intr)
## Lg.UK.CDcnt -0.388
```

How do you report a mixed-effects model?

- Explain what variables went into the analysis: say what the outcome and predictor variables were
- ullet Report the model equation RT \sim frequency + (frequency + 1 || participant) + (1 | word)
- Report a table of coefficients: variable, estimate of coefficient of effect; SE; t (or z); and p
- Add to that table a report of the random effects terms: variances
- You should comment on the coefficient estimates; you may (or may not) comment on the random effects variances

Next week: we need to be ready to trouble shoot

- I stopped the model from estimating the covariance between random effects of participants on items and on slopes
- ullet using (frequency $+\ 1\ ||\ \mathsf{participant})$ not (frequency $+\ 1\ |\ \mathsf{participant})$
- next week I explain why: convergence

Summary – Week 18: crossed random effects

- Psychological studies often have repeated measures designs
 - When there are multiple observations for each person or stimulus
 - Because each person has to respond to multiple stimuli
 - And each stimulus is shown to multiple people
- Mixed-effects models can be specified by the researcher
 - to account for random differences between participants or between stimuli
 - in the intercepts or the slopes of explanatory variables

Human diversity and how people vary: the challenge, the promise

- Variation is a fact and mixed-effects models enable us to take into account random differences between people
- But these models also allow us this is new to examine the nature of the variation directly

