

# The linear model

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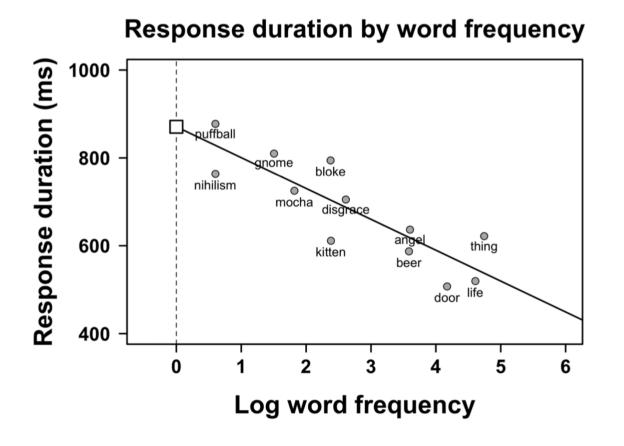
# Outline

- Regression line: intercept and slope.
- Residuals
- Different types of regression
- Assumptions
- Measuring model fit: R<sup>2</sup>





## An example: Word frequency effects







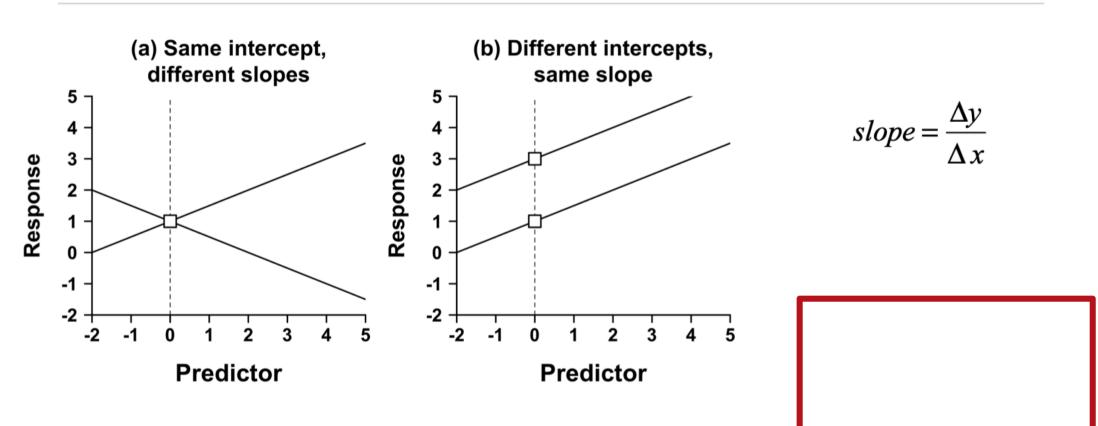
# Terminology

У	x
response/outcome dependent variable	predictor independent variable explanatory variable regressor



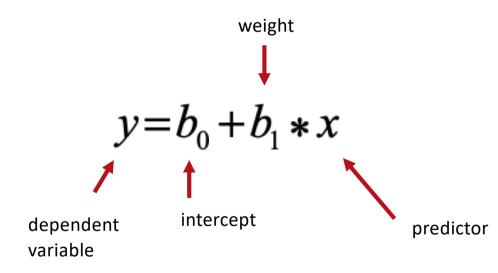


# Specifying a line: Slope and intercept





#### **Regression line**







# An example: Word frequency effects (2)

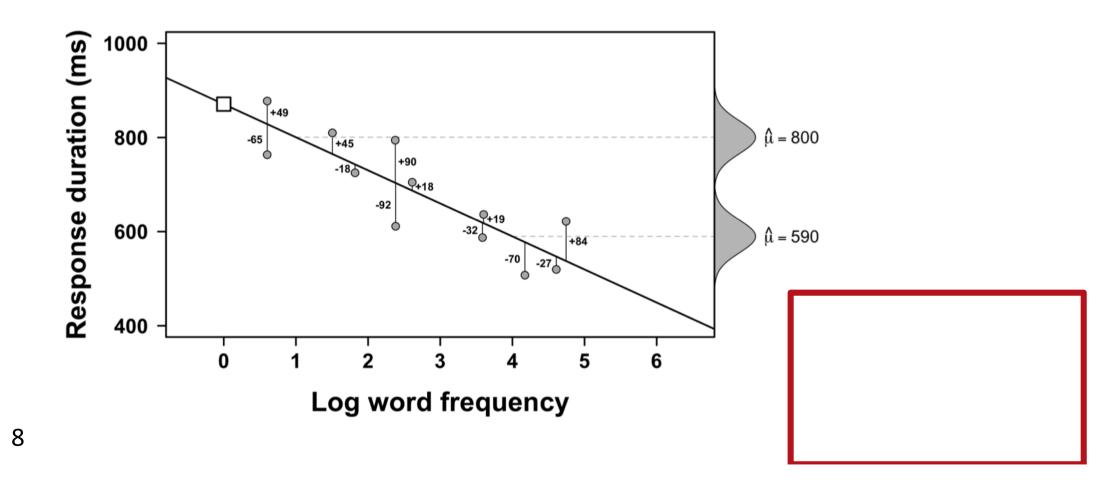
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#### Response duration (ms) 1000 $y = b_0 + b_1 * x$ 800 \_\_\_\_ nihilism response duration = $880ms + \left(-70\frac{ms}{freq}\right) * word frequency$ © thing 600 kitten beer © life $\circ$ door 400 2 0 1 3 5 response duration = $880ms + \left(-70\frac{ms}{freq}\right) * 3 freq = 670ms$ Log word frequency

#### Response duration by word frequency

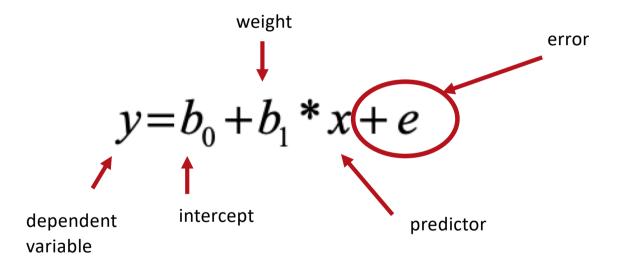


#### Residuals





## Regression line (2)







## Linear regression

... is a statistical method used to create a linear model

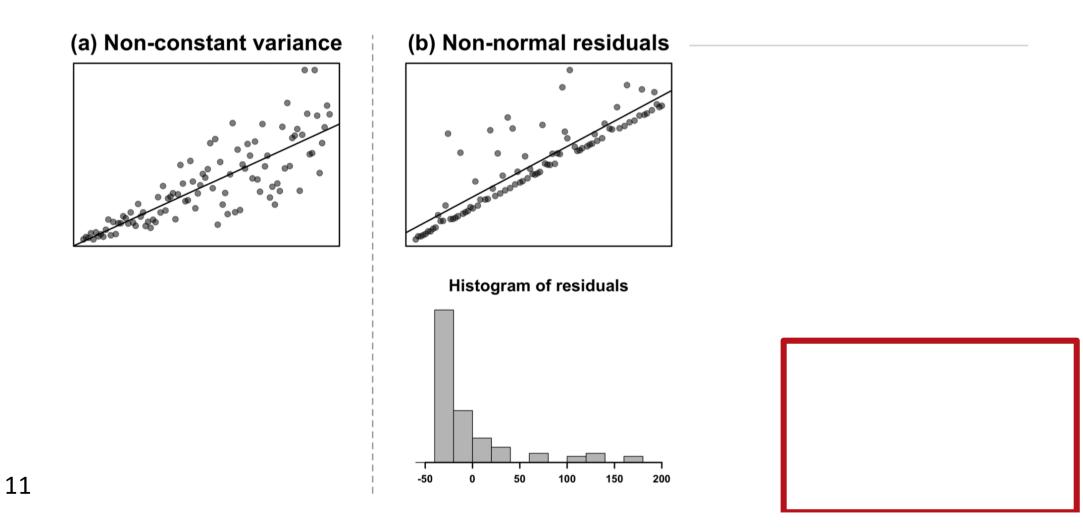
... there are different types:

- Simple linear regression: models using only one predictor
- Multiple linear regression: models using multiple predictors
- Logistic regression: models a categorical response variable
- Multivariate linear regression: models for multiple response variables



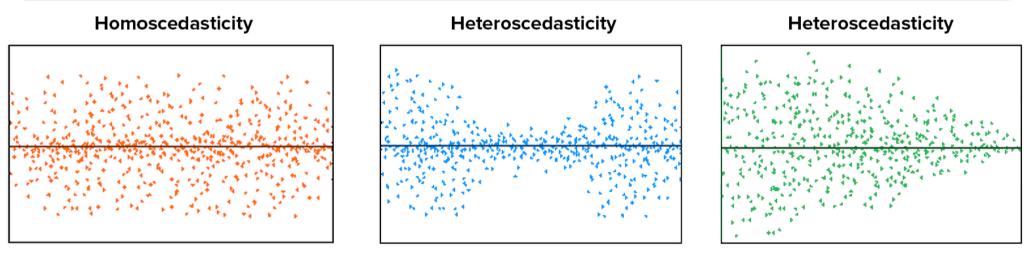


#### Assumptions





## Homoscedasticity



Random Cloud (No Discernible Pattern)

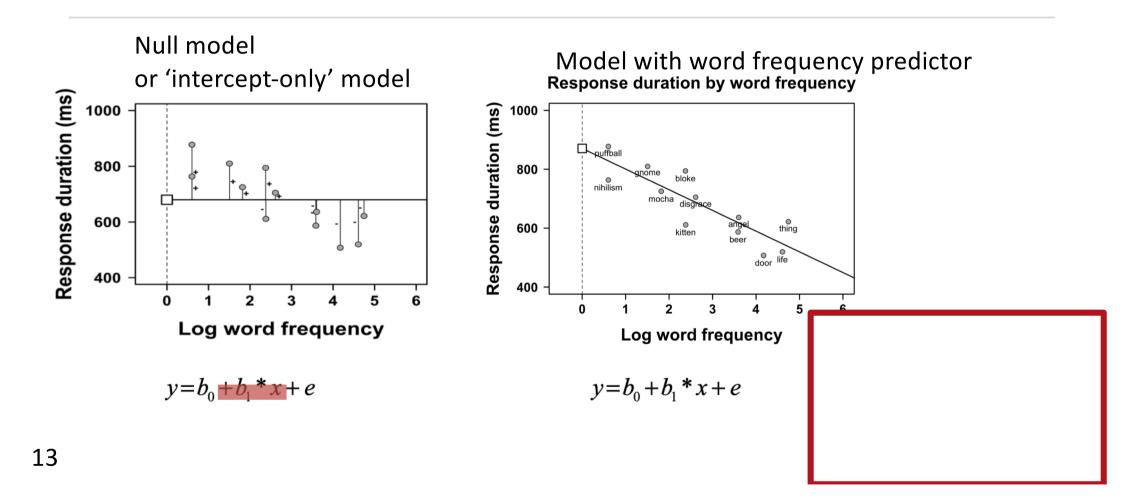
Bow Tie Shape (Pattern)

Fan Shape (Pattern)



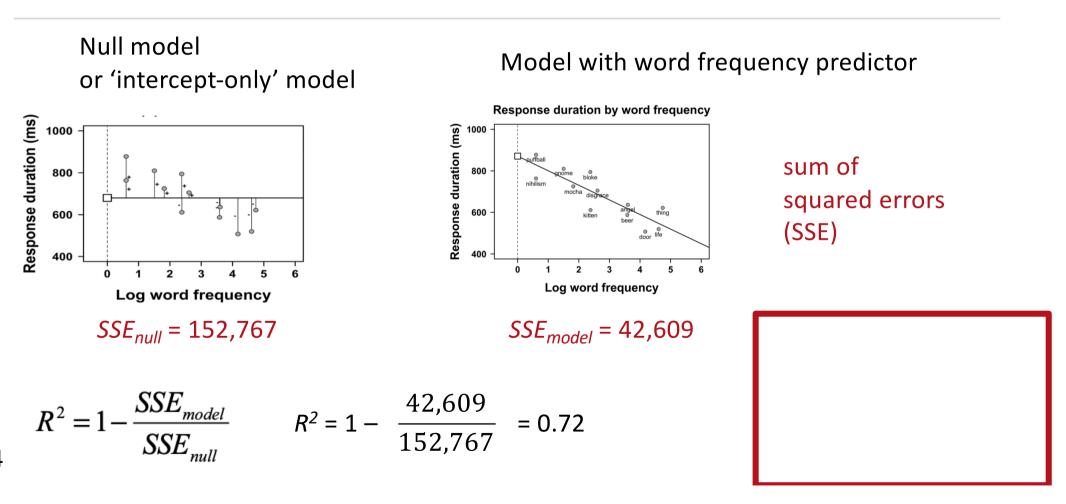


# Measuring model fit: The null model



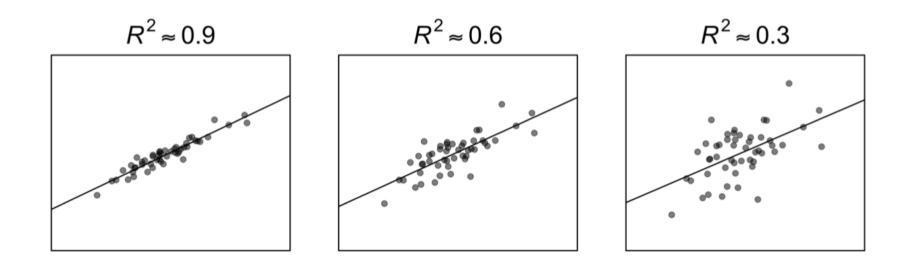


# Measuring model fit: R-squared





# Measuring model fit: R-squared (cont.)



 $R^2$  is a measure of effect size.

 $R^2$  values range from 0 to 1.

Values closer to 1 indicate better model fits as well as stronger effects.



## Summary

- Mathematical specification of a line: intercept and slope.
- Regression line formula:
- Residuals = observed values fitted values
- Simple linear regression, multiple linear regression, logistic regression, multivariate regression
- Assumptions: <u>residuals</u> need to be normally distributed and show constant variance (i.e., be homoscedastic)
- *R*<sup>2</sup> uses the residuals of the null model to standardise the residuals of the main model. This provides an effect size and tells us what proportion of variation in the dependent variable can be accounted for by the predictor in the main model.

